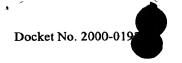# OFDM COMMUNICATION SYSTEM AND METHOD HAVING A REDUCED PEAK-TO-AVERAGE POWER RATIO

5   CROSS REFERENCE TO RELATED APPLICATIONS

This application claims the benefit of U.S. Provisional Application No. 60/192,708, filed on March 28, 2000.

STATEMENT REGARDING FEDERALLY SPONSORED RESEARCH

10   Not Applicable.

FIELD OF THE INVENTION

The present invention relates generally to communication systems and, more particularly, to Orthogonal Frequency Division Multiplexing (OFDM) wireless

15   communication systems.

BACKGROUND OF THE INVENTION

Orthogonal frequency division multiplexing (OFDM) wireless communication systems have desirable characteristics for high-bit-rate transmission in a radio

20   environment. For example, by dividing the total bandwidth into many narrow subchannels, which are transmitted in parallel, the effects of multipath delay spread can be minimized. OFDM systems have been adopted or proposed for Digital Audio Broadcasting, Digital Terrestrial Television Broadcasting, wireless LANs, and high-speed cellular data.

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One disadvantage of using OFDM techniques for wireless applications is the potentially large peak-to-average power ratio (PAP) characteristic of a multicarrier signal with a large number of subchannels. For example, a baseband OFDM signal with N subchannels has a PAP equal to the number of subchannels squared divided by the

30   number of subchannels, i.e., $PAP=N^2/N=N$. For N = 256, the PAP≈24 dB. When passed

through a nonlinear device, such as a transmit power amplifier, the signal may suffer significant spectral spreading and in-band distortion.

Conventional solutions to reducing the PAP for OFDM systems include using a
5   linear amplifier and using a non-linear amplifier while backing off the amplifier operating point. However, these approaches result in a significant power efficiency penalty.

Another attempt to reduce the PAP includes deliberately clipping the OFDM signal before amplification to improve the PAP at the expense of some performance
10 degradation. Another technique uses nonlinear block coding, where the desired data sequence is embedded in a larger sequence and only a subset of all the possible sequences are used, specifically those with low peak powers. Using this approach, a 3 dB PAP can be achieved with a relatively small bandwidth penalty. However, to implement such a coding scheme, large look-up tables are required at the transmitter and the receiver,
15 thereby limiting its usefulness to applications with a small number of subchannels. Progress has been made toward coding schemes that reduce the PAP and can be implemented in a systematic form with some error- correcting capabilities. Nevertheless, these methods are difficult to extend to systems with more than a few subchannels and the coding gains are relatively small for adequate levels of redundancy.
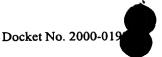20

Additional techniques for improving the statistics of the PAP of an OFDM signal include selective mapping (SLM) and partial transmit sequence (PTS). In SLM, a predetermined number M of statistically independent sequences are generated from the same information and the sequence with the lowest PAP is chosen for transmission.
25 However, this introduces additional complexity for providing improved PAP statistics for the OFDM signal. In addition, the receiver must have knowledge about the generation process of the transmitted OFDM signal in order to recover the information. The sequence information is sent as side information, resulting in some loss of efficiency.

It would, therefore, be desirable to provide an OFDM system having a reduced PAP with optimal efficiency.

SUMMARY OF THE INVENTION

5   The present invention provides an OFDM system that embeds PAP-reducing inversion sequence information in the transmitted signal with no additional overhead. With this arrangement, the PAP ratio of the transmitted signals is reduced with little or no impact on the overall system efficiency. While the invention is primarily shown and described in conjunction with an OFDM system, it is understood that the invention is

10   applicable to other systems in which it is desirable to detect embedded sequence information.

        In one aspect of the invention, in an OFDM system a block of symbols is partitioned into a predetermined number of clusters. A respective phase factor is

15   generated for each cluster to form an inversion sequence that reduces the PAP of the transmitted signals. A variety of techniques can be used to generate the inversion sequence including suboptimal iterative algorithms and optimum approximations, which can correspond to Walsh sequences for example. The inversion sequence is embedded onto the transmitted data by rotating selected ones of the tones in a cluster based upon

20   whether the cluster phase factor rotates the cluster. In one embodiment, binary phase factors, i.e., plus/minus one, are used. If the inversion sequence does not rotate the cluster, i.e., the cluster phase factor is plus one, then none of the tones in the cluster are rotated. If the inversion sequence does rotate the cluster, i.e., the cluster phase factor is minus one, then every other tone in the cluster is rotated by a predetermined amount, e.g.,

25       $\pi/4$ radians.

        To detect the inversion sequence, the receiver first removes the data modulation. A test statistic is then generated for each cluster. The test statistics can be used to make decisions in a variety of ways including quantizing the test statistic and making

30   independent decisions for each cluster, quantizing the test statistics and decoding the

entire sequence by nearest Hamming distance, and decoding the sequence by nearest Euclidean distance.
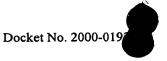
BRIEF DESCRIPTION OF THE DRAWINGS

5   The invention will be more fully understood from the following detailed description taken in conjunction with the accompanying drawings, in which:

FIG. 1 is a top level diagram of an OFDM system having reduced PAP in accordance with the present invention;

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FIG. 2 is a pictorial representation of OFDM subcarriers that can be generated by the OFDM system of FIG. 1;

FIG. 3 is a pictorial representation of orthogonal OFDM subcarriers that can be

15   generated by the OFDM system of FIG. 1;

FIG. 4 is a schematic representation of a portion of an OFDM system that embeds inversion sequence information in the transmitted signals in accordance with the present invention;

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FIG. 5 is a flow diagram of an exemplary sequence of steps for providing an optimal PAP for an OFDM system in accordance with the present invention;

FIG. 6 is a graphical depiction showing the probability of error in detecting an

25   inversion sequence embedded in the transmitted signals in accordance with the present invention; and

FIG. 7 is a graphical depiction of detection performance for an OFDM system in accordance with the present invention.

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DETAILED DESCRIPTION OF THE INVENTION

The present invention provides a technique for achieving high-bit-rate wireless data transmission in an orthogonal frequency division muliplexing (OFDM) system with
5   a relatively low peak-to-average power ratio (PAP). The system utilizes partial transmit sequences for providing favorable PAP statistics with combining sequence information embedded in the transmitted data. With this arrangement, no overhead is required to provide the combining sequence information to the receiver.

10   FIG. 1 shows an exemplary OFDM system 100 having sequence data embedded in the transmitted data in accordance with the present invention. The system 100 includes components for transmission and reception of data. A coding subsystem 102 encodes binary data from a data source. The coded data is interleaved by an interleaving subsystem 104 and then mapped onto multi-amplitude multi-phase constellation symbols
15   by a mapping subsystem 106. In one particular embodiment, the multi-amplitude multi-phase constellation symbols include quadrature phase shift keying (QPSK) symbols. Pilot signals can then be inserted by a pilot insertion subsystem 108 to estimate the channel at the remote subscriber unit receivers. A serial-to-parallel conversion subsystem 110 converts the serial data stream to a parallel data stream that is provided to an inverse
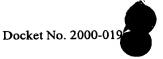20   fast fourier transform (IFFT) subsystem 112.

The transformed data is converted to serial data stream by a parallel-to-serial converter 114. Cyclic extension and windowing can be added by a subsystem 116 prior to digital-to-analog conversion by a DAC 118 and transmission by an antenna 120
25   system. A receive portion 130 of the OFDM system includes corresponding components for extracting the data from the received OFDM signal.

As shown in FIG. 2, the OFDM system 100 utilizes an overlapping orthogonal multicarrier modulation technique having a plurality of subcarriers 150. FIG. 3 shows the
30   orthogonal relationship of the subcarriers. More particularly, each of four subcarriers

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160a-160d of one OFDM data symbol has an integral number of cycles in the interval T. The number of cycles between adjacent subcarriers differs by one.

5   FIG. 4 shows a portion of an OFDM system 200 that embeds PAP-reducing inversion sequence information within the transmitted data with no overhead in accordance with the present invention. With this arrangement, the need to dedicate reference subcarriers, e.g., one for each cluster, to transmit phase factor information is eliminated.

10   The OFDM system 200 includes a data source 202 generating a data stream X that is converted from a serial stream to a plurality of parallel data streams X_1-X_M and partitioned by a subsystem 204 as described below. The partitioned data streams are transformed by respective inverse fast Fourier transform systems 206_1-206_M, in a conventional manner The clusters of transformed data are rotated by respective phase

15   factors b_1-b_m, which are embedded into the transmitted data, as described below in detail. An optimizer subsystem 208 can facilitate selection of the phase factors that reduce the PAP ration of the transmitted OFDM signals.

    Initially, a block of N symbols $\{X_n, n=0,\dots,N-1\}$ is formed with each symbol

20   modulating one of a set of N subcarriers, $\{f_n, n=0, 1,\dots, N-1\}$. The N subcarriers are chosen to be orthogonal, i.e., $f_n = n\Delta f$, where $\Delta f= 1/NT$ and T is the original symbol period, as shown in FIG. 3. The resulting signal after D/A conversion can be expressed as set forth below in Equation 1:

$$x(t) = \sum_{n=0}^{N-1} X_n e^{j2\pi f_n t} \; , \; 0 \# t \# NT \qquad\qquad \text{Eq. (1)}$$

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The PAP of the transmitted signal from Equation (1) can be defined as shown in Equation (2) below:

$$PAP = \frac{\max|x(t)|^2}{E\left[|x(t)|^2\right]}$$

Eq. (2)

5   To obtain the partial transmit sequence (PTS), the input data block is partitioned into disjoint sub-blocks or clusters by subsystem 204 which are combined to minimize the PAP. A data block is defined as $\{X_n, n=0, 1,\ldots, N-1\}$, which can be represented as a vector $X=[X_0\ X_1\ \ldots\ X_{N-1}]^T$, where T is the symbol period. The vector X is partitioned into a predetermined number M of disjoint sets represented by vectors $\{X_m, m=1,2,\ldots M\}$.

10   The partial transmit sequence technique forms a weighted combination of M clusters as set forth below in Equation 3:

$$X' = \sum_{m=1}^{M} b_m X_m$$

Eq. (3)

where $\{b_m, m=1, 2,\ldots, M\}$ are phase or weighting factors, which can be pure rotations. In

15   the time domain, this relationship can be represented as shown in Equation 4 below:

$$x' = \sum_{m=1}^{M} b_m x_m$$

Eq. (4)

The vector x_m, which is referred to as the partial transmit sequence, is the Inverse Fast Fourier Transform (IFFT) of vector X_m. The phase factors b_m are chosen to minimize the PAP of x', as described below.

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The phase factors can be generated in a variety of ways to minimize the PAP of the transmitted OFDM signals, including optimization, iteration, and random generation. For example, a predetermined number of Walsh sequences can be generated.

25   In one particular embodiment, the phase factors b_m are binary phase factors, i.e., ± 1. In an alternative, more complex embodiment, the phase factors include ± 1 and $\pm j$. After the input data block is divided into a predetermined number M of clusters, the M N-
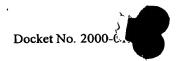
point partial transmit sequences are formed. For example, an OFDM system having 256 subcarriers can include sixteen (M=16) data clusters each having sixteen subcarriers.

FIG. 5 shows an exemplary sequence of steps for determining binary phase factors for the partial transmit sequence. In step 300, the phase factors b_m are set to be one for all m and in step 302 the PAP (PAP$_0$) of the combined signal with all phase factors set to one is computed. In step 304, the phase factor index m is set to 1.

In step 306, the first phase factor b_1 is inverted, i.e., b_1=-1, and the PAP is re-computed with inverted phase factor in step 308. In step 310, is it determined whether the new PAP value is lower than the original PAP$_0$. If it is lower, then in step 312 the first phase factor b_1 remains minus one as part of the final phase sequence $\{b_m, m=1,...,M\}$. If it is not lower, in step 314 the first phase factor is reset to one, i.e., b_1=1. In step 316, the index value M is examined and in step 318 the index value is incremented until each phase factor is determined to be a one or a minus one.

Alternatively, a predetermined number of random sequences, which can be Walsh sequences, are selected. The information sequence is multiplied by a predetermined number of the sequences. The result providing the best PAP characteristics is then selected. This approach approximates an optimum PAP as described in L.J. Cimini. Jr. and N.R. Sollenberger, "Peak-to-Average Power Ration Reduction of an OFDM Signal Using Partial Transmit Sequences," *IEEE Commun. Letts.*, Vol. 4, No. 3, March 2000, pp. 390-393, which is incorporated herein by reference.

FIG. 6 shows the PAP versus CCDF simulated results for an OFDM system having 256 subcarriers with the transmitted signal oversampled by a factor of four. QPSK signal modulation is assumed with the energy normalized to unity. Results are shown for the case of a single OFDM block (M=1) and for 16 clusters (M=16) each including 16 subcarriers. The unmodified OFDM signal has a PAP that exceeds 10.4 dB for less than 1% of the blocks. For the suboptimal algorithm using 16 Walsh sequences

of length 16 as the inversion sequence, a value of about 8 dB is obtained. By using the PTS approach with the optimum binary phase sequence for combining, the 1% PAP reduces to 6.8 dB. While a degradation of about 1 dB is encountered using the suboptimal approach, the optimization process has been reduced to 16 sets of 16

5   additions, a significant savings as compared to finding the optimum set of phase factors.

To recover the data, the OFDM system receiver determines the inversion sequence that was embedded in the transmitted signals. In contrast to known systems that send inversion sequencing information as explicit side information (via subcarriers) at the

10   expense of some loss in efficiency, an OFDM system in accordance with the present invention embeds a marker onto the transmitted data that can be used to uniquely identify the inversion sequence at the receiver. The detection of the inversion sequence should be sufficiently reliable so as not to have a significant effect on the overall system performance.

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As described above, the OFDM system embeds markers on the transmitted signals. In an exemplary embodiment described above, if the inversion sequence does not rotate the cluster, e.g., $b_m = 1$, then no tones in the cluster are rotated. If the inversion sequence rotates the cluster, e.g., $b_m = -1$, then every other tone in that cluster is rotated by

20   $\pi/4$ radians. This arrangement is equivalent to using two signal constellations for the data symbols in a cluster: one for the unrotated clusters and another, rotated by $\pi/4$, for the modified clusters. This algorithm puts an embedded marker on rotated clusters that can be reliably detected even in the presence of noise and multipath fading with a minimal impact on the overall system performance.

25

To detect the inversion sequence, the data modulation must first be removed. In an illustrative embodiment, the frequency symbols are raised to the fourth power, which is a standard approach for removing QPSK modulation. Higher-order PSK modulations can be removed in a similar fashion, as is well known to one of ordinary skill in the art.

30   With the modulation removed, the data symbols (in the frequency domain) can be

differentially detected by computing, for each cluster, a test statistic as set forth below in Equation 5:

$$Z_m = \sum_{j=1}^{N/M-1} (Y_{j,m} Y^*_{j+1,m})^4 \qquad \text{Eq. (5)}$$

where $Y_{j,m}$ represents the jth tone in the mth cluster and * denotes conjugation. Thus, in the absence of noise, if cluster m was not altered by the inversion sequence, then the mth test statistic Z_m is +(N/M-1). If $b_m = -1$, then Z_m is - (N/M-1). Therefore, a relatively simple binary detection scheme can recover the inversion sequence. The summation over the tones in a cluster averages the noise and provides a significant performance improvement.

Given the decision statistic in Equation 5, a variety of detection schemes can be used. In one embodiment, the test statistic is quantized to ±1 and decisions are made independently for each cluster. While this approach is relatively simple, there is no straightforward mechanism for correcting errors.

In another embodiment, detection performance is improved by quantizing the individual test statistics Z_m and then decoding the entire sequence to the nearest sequence, e.g., Walsh sequence. Specifically, the system first generates the sequence {Re[Z_m], m=1,2,...,M} and quantizes each component to +1 or -1. The system then chooses the Walsh sequence of length M that is closest, in Hamming distance, to the resulting sequence. This technique provides error correction since the received sequence is mapped into one of only M possible Walsh sequences.

In a further embodiment that provides further performance improvements, all of the information in the decision statistics is retained. Therefore, one preferred strategy is to compute the sequence {Z_m, m=1,2,...,M} and then choose the Walsh sequence of length M that is closest, in Euclidean distance, to the resulting sequence.